

Analytical Performance Evaluation of Cooperative and Multi-Radio Concepts in Emerging Wireless Networks

W.I.N.T.E.R. Group

*Olga Galinina, PhD candidate
Tampere University of Technology*

IEEE Montreal Section, Concordia University

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Motivation



1. **5G**: integration of diverse techniques and solutions to improve performance of wireless systems
2. **Multi-RAT**: Multiple radios and associated device/ infrastructure intelligence will become a fundamental characteristic of 5G
3. **Cooperation**: Use of centralized cellular connectivity will help to manage direct links

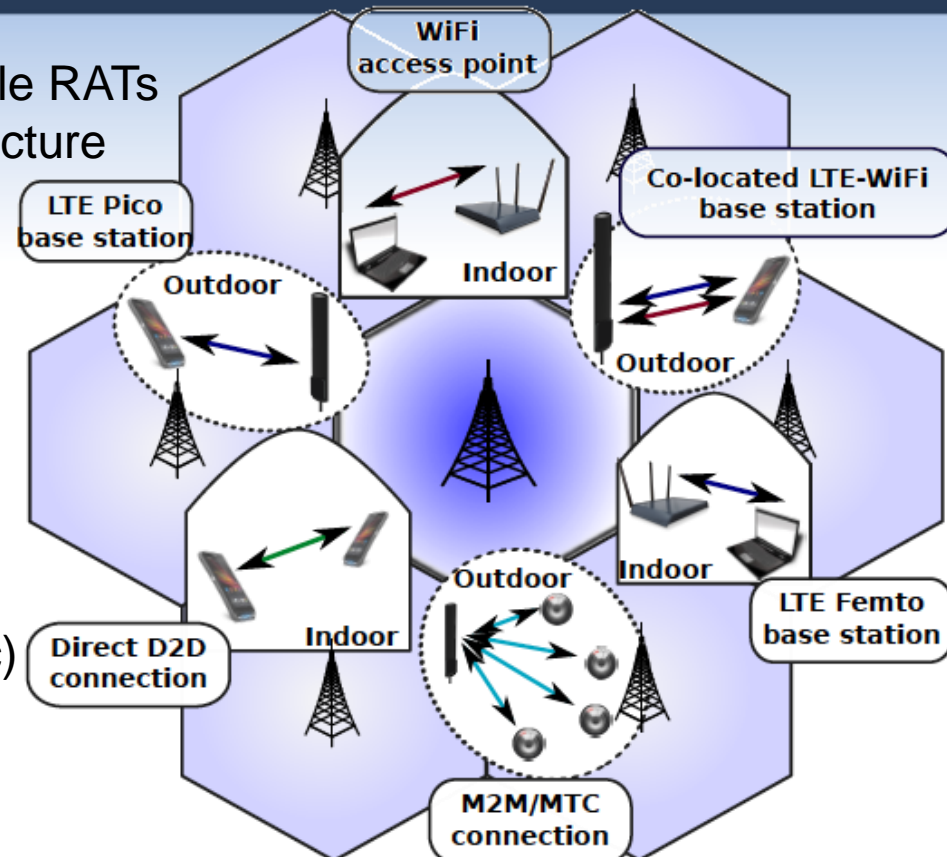


Focus and Contributions of Proposed Research

Environment: integration between multiple RATs (WLAN and D2D) within HetNet architecture

Target: a predictor of flow-level **uplink** performance (stochastic traffic loads)

- Real-time data sessions with the minimum bitrate
- Files of random size (elastic traffic)



Evaluating: blocking probabilities/average number of users/energy consumption/...

Result: unified **Space-Time** methodology for modeling HetNet operation



Origin of the Proposed Mathematical Approach

TIME

QUEUEING THEORY



Erlang published his first paper on queueing theory in 1909

SPACE

STOCHASTIC GEOMETRY



geometric probability

Name is proposed by Frisch and Hammersley in 1963 as a name of a theory of "random irregular structures"



Methodology for Space-Time Network Analysis



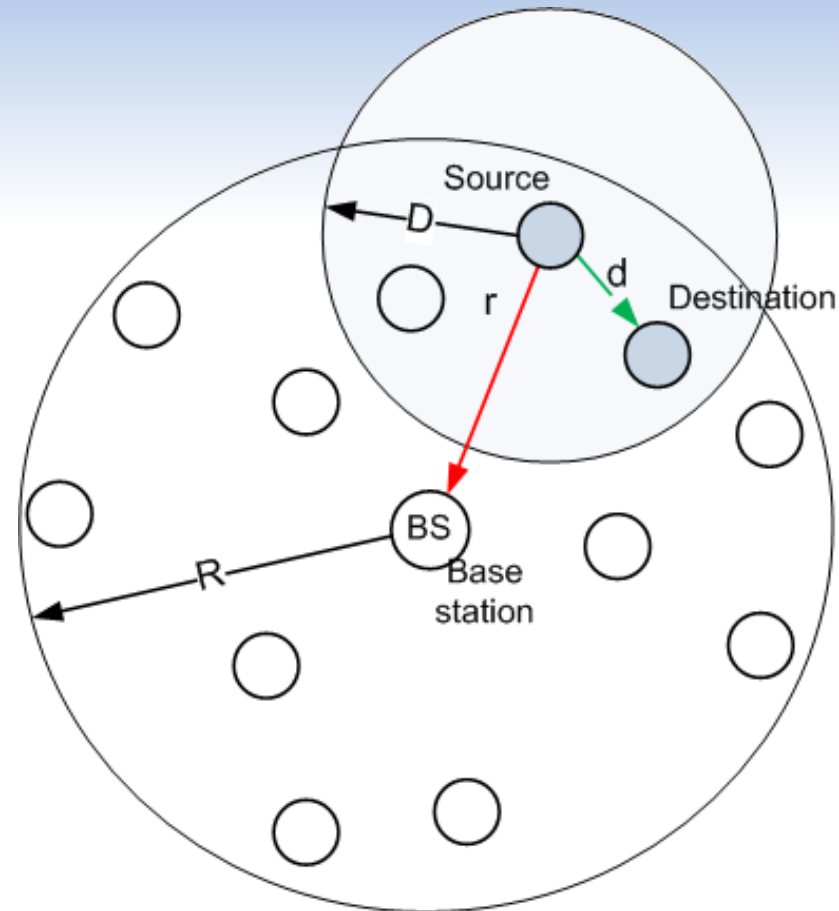
Baseline model



Spatial network model: baseline

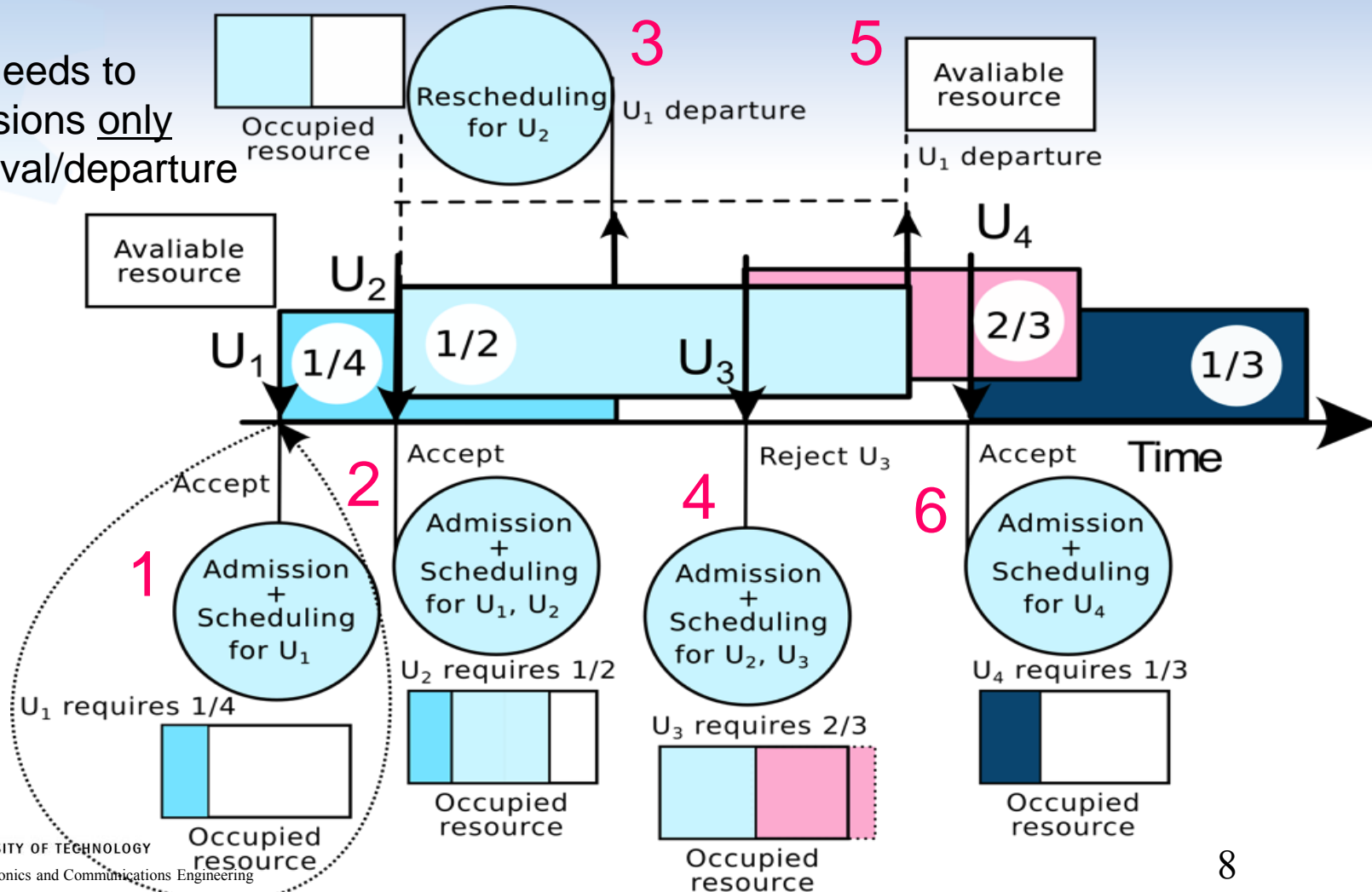
System model

1. Circle (sector) of radius R , base station.
2. Uniform user location,
different channel characteristics.
 - Poisson arrivals of flows/sessions, λ
 - constant target bitrate, r
 - exponential holding time, μ
3. Admission/power control



Flow-level dynamic example

Predictor needs to make decisions only at user arrival/departure



Power/rate model

Assumption

The channel gain between Tx i and Rx j depends on the distance between them:

$$\gamma_{i,j} = \frac{G}{d_{i,j}^k}$$

k is *propagation exponent*,
 G is *propagation constant*.

Assumption

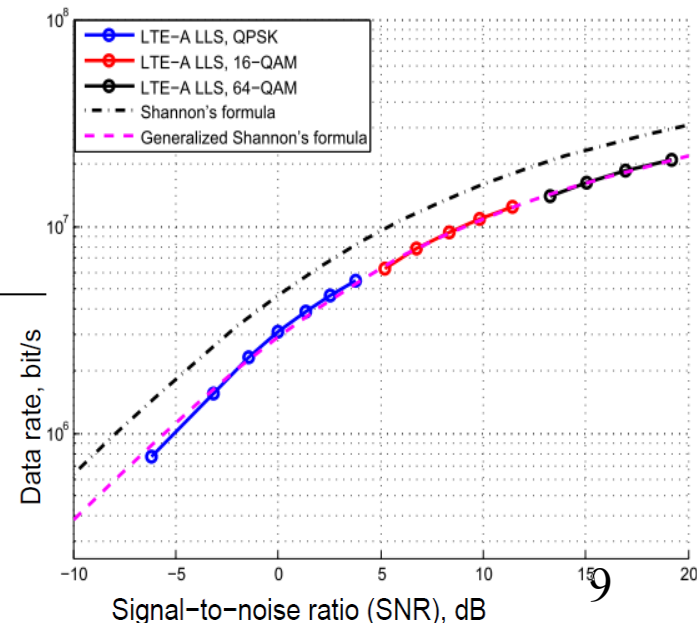
User transmit power and rate are coupled by *Shannon's formula*:

$$r_i = B \log(1 + Ap_i)$$

p_i is output power of the RF power amplifier,
 A, B are additional parameters, depending on
wireless system implementation and configuration

$$A = \frac{\eta\gamma_{i,i}}{N_0 + I}, \quad B = w$$

Shannon's formula
for QPSK, 16-QAM, 64-QAM



Power/resource allocation

Assumption:

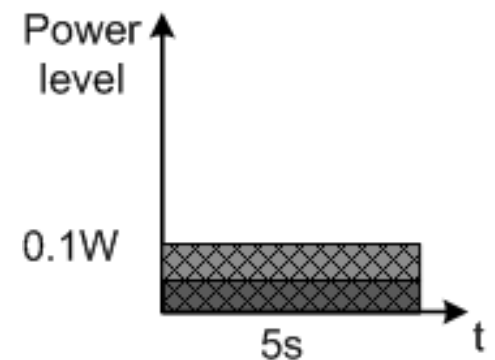
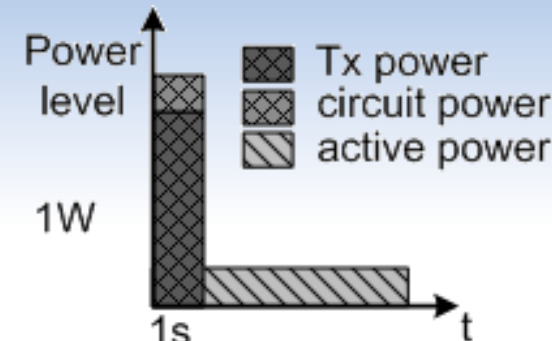
Three different power levels for every transmitter:

- transmit power consumption p_i
- circuit power p_c ,
- active power consumption p_a
- idle power consumption (set for simplicity $p_{idle} = 0$)

Assumption (power/resource allocation policies):

1. “Maximum power” = fixed maximum power
2. “Full utilization” = system resource is used completely
Each session is allocated resource portion

(n users in service adjust transmit power to match target bitrate r_0)



$$\frac{r_0}{r_i} = \frac{1}{n}$$



System model analysis

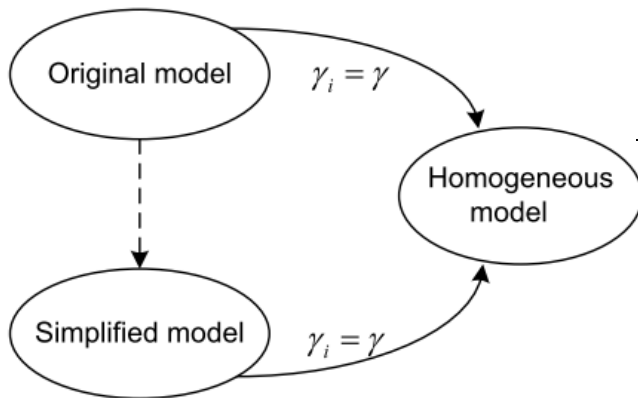
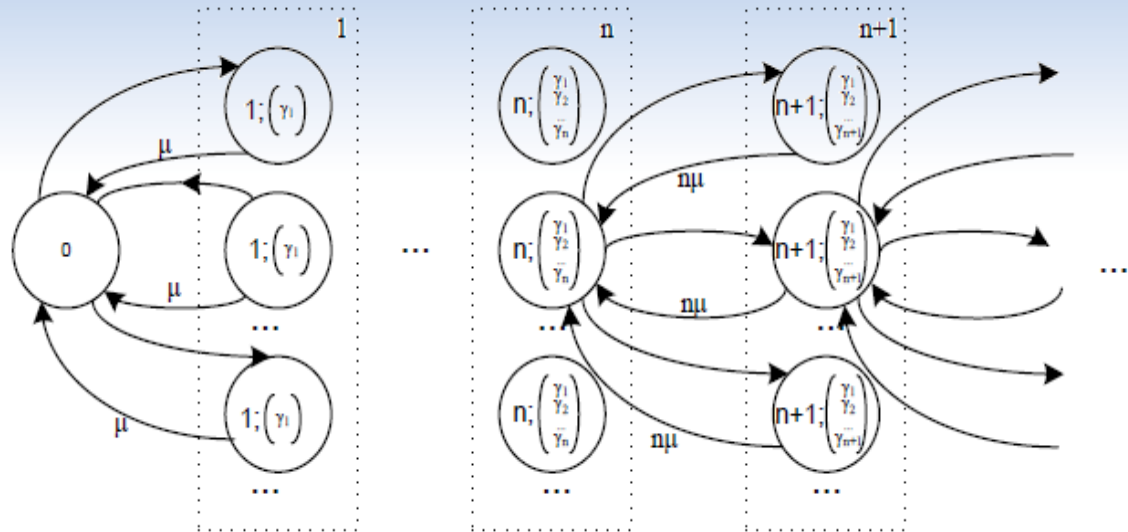
1. Describe and analyze the **generalized system model**

2. Markov process $S(t)$:
number of users + vector SNR

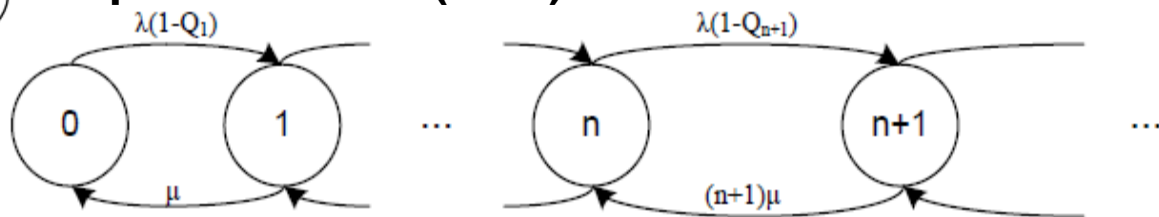
$$n, (\gamma_1, \dots, \gamma_n)$$

3. Set of states is uncountable

Use state aggregation



Simplified model (BDP)



4. Steady-state distribution via calculating all probability integrals

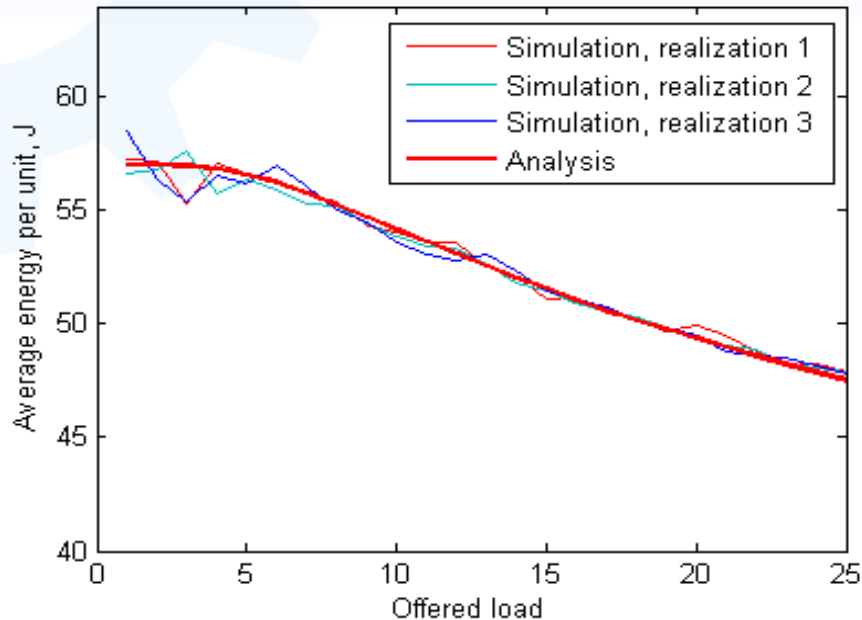
Q_{n+1} - probability of rejection at the stage n



Numerical results

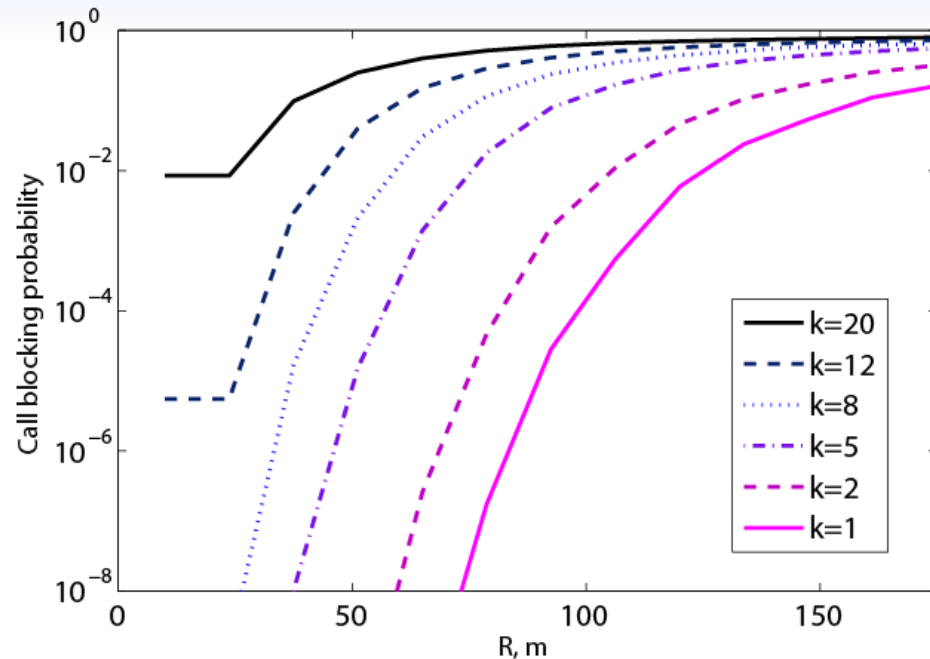
Average energy consumption (per flow), $E[J]$

$$E[J] = \frac{E[P]}{\lambda(1 - P_{block})}$$



Average energy vs. offered load

Blocking probability



Blocking probability vs. distance (FU)



Proposed methodology



“Construction toy” for UL performance prediction

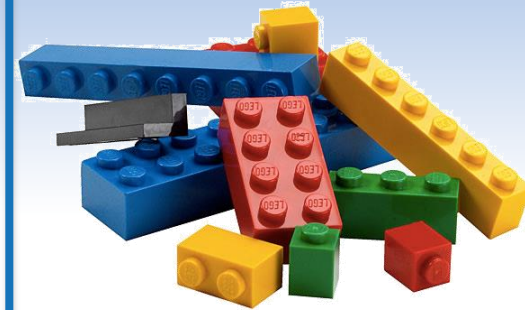
Blocks:

Space

Spatial distribution of infrastructure

Spatial distribution of users

Area of interest



“Construction toy” for UL performance prediction

Blocks:

Space

Spatial distribution of infrastructure

Spatial distribution of users

Area of interest

- Poisson point process (PPP)
- Poisson cluster process
- Hard core point process
- Determinantal (e.g. Ginibre)
- ...



“Construction toy” for UL performance prediction

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Space

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“Construction toy” for UL performance prediction

Blocks:

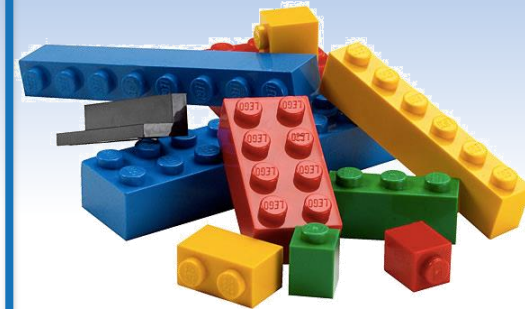
Space

Spatial distribution of infrastructure

Spatial distribution of users

Area of interest

- Circle
- Voronoi cell
- Hexagon
- ...



“Construction toy” for UL performance prediction

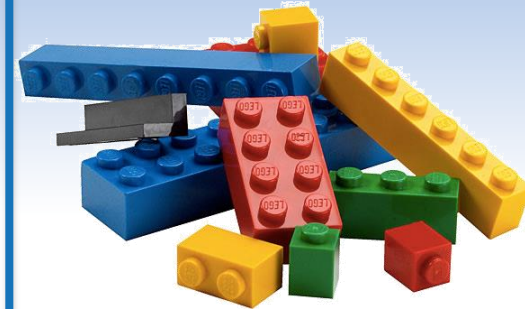
Blocks:

Space

Spatial distribution of infrastructure

Spatial distribution of users

Area of interest



[Outcomes]



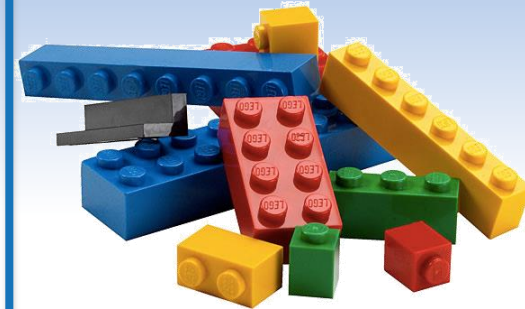
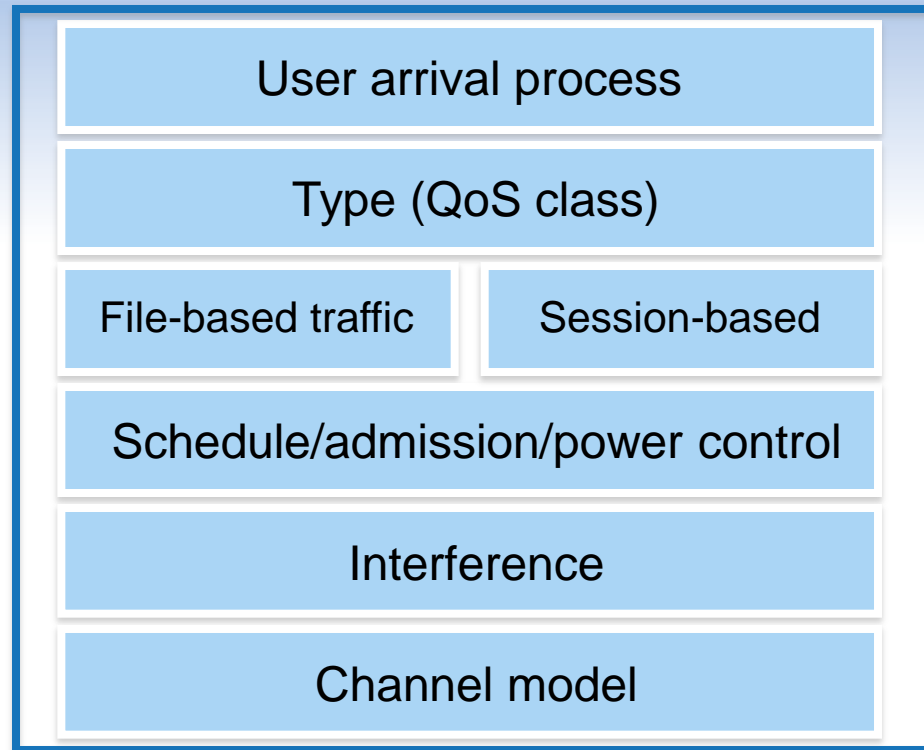
- Distribution of the **distance** between transmitters and receivers
- Distribution of the **instantaneous rates**
- Distribution of the **actual transmission rates**
- Distribution of **occupied individual shares** of the total resource
- Distribution of the **total occupied resource**



“Construction toy” for UL performance prediction

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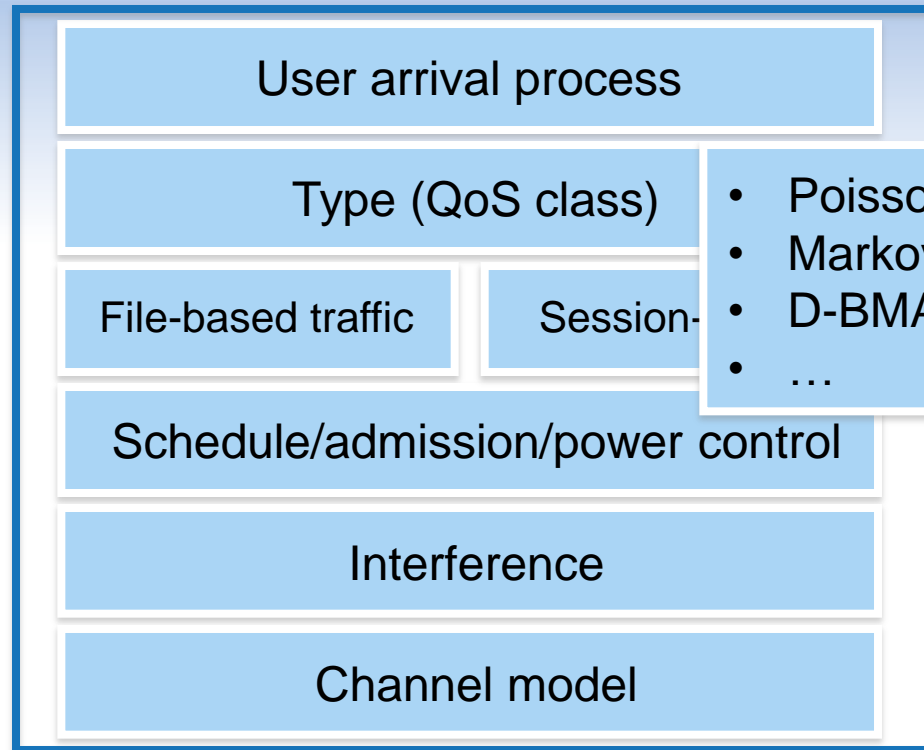
Time



“Construction toy” for UL performance prediction

Blocks:

Time



“Construction toy” for UL performance prediction

Blocks:

Time

User arrival process

Type (QoS class)

File-based traffic

Session-based

- Exponential file size
- Erlang-k file size
- Heavy-tailed distributions
- ...

Transmission/power control

Interference

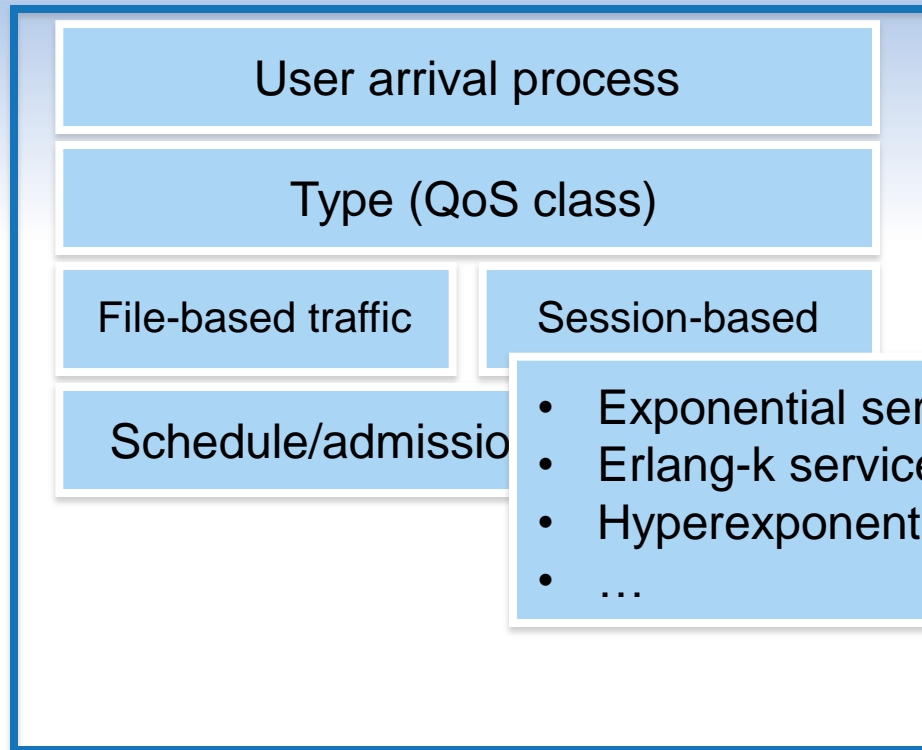
Channel model



“Construction toy” for UL performance prediction

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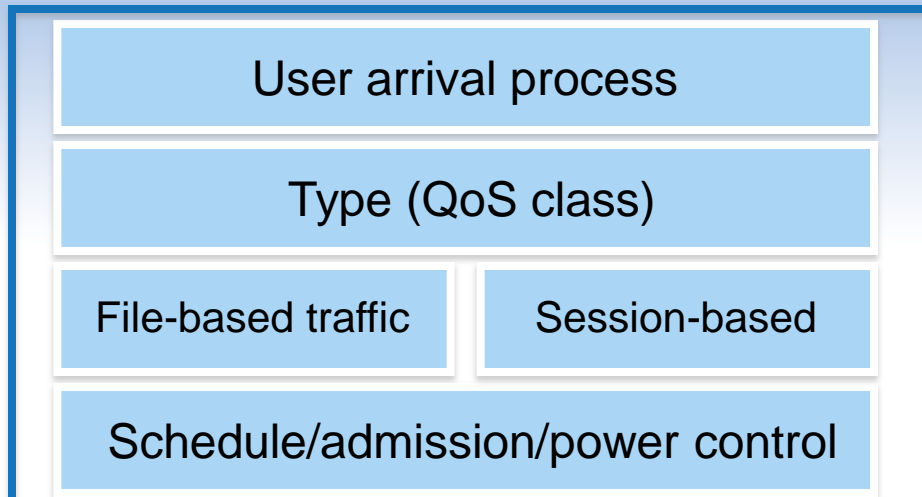
Time



“Construction toy” for UL performance prediction

Blocks:

Time



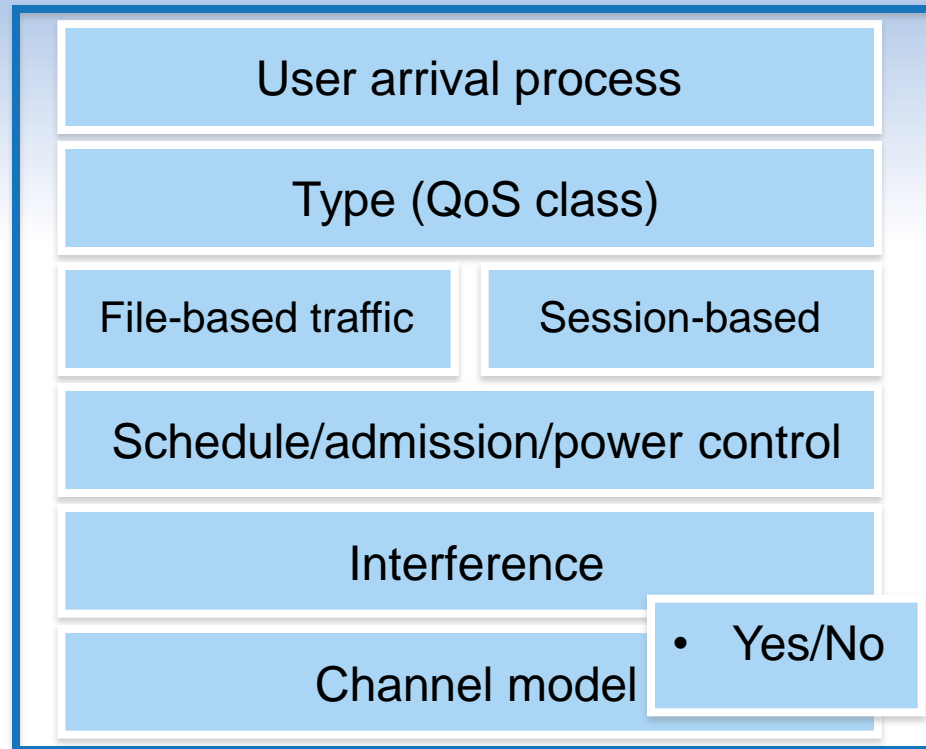
- Round robin
- Weighted RR
- ...
- Check resource
- Check bitrate
- ...
- Fixed power
- Power control
- ...



“Construction toy” for UL performance prediction

Blocks:

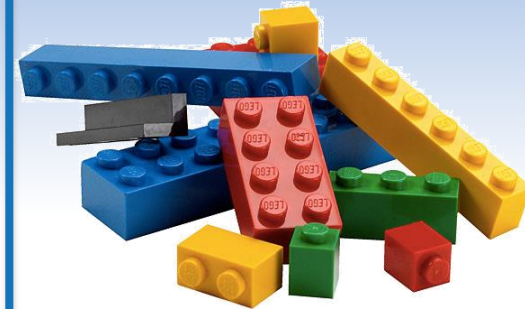
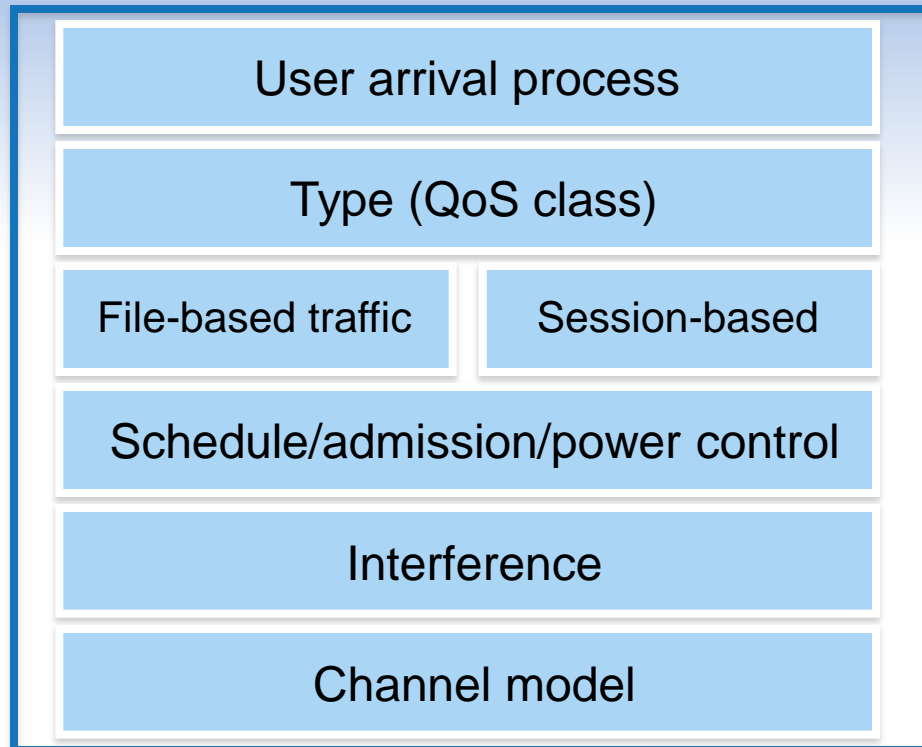
Time



“Construction toy” for UL performance prediction

Blocks:

Time



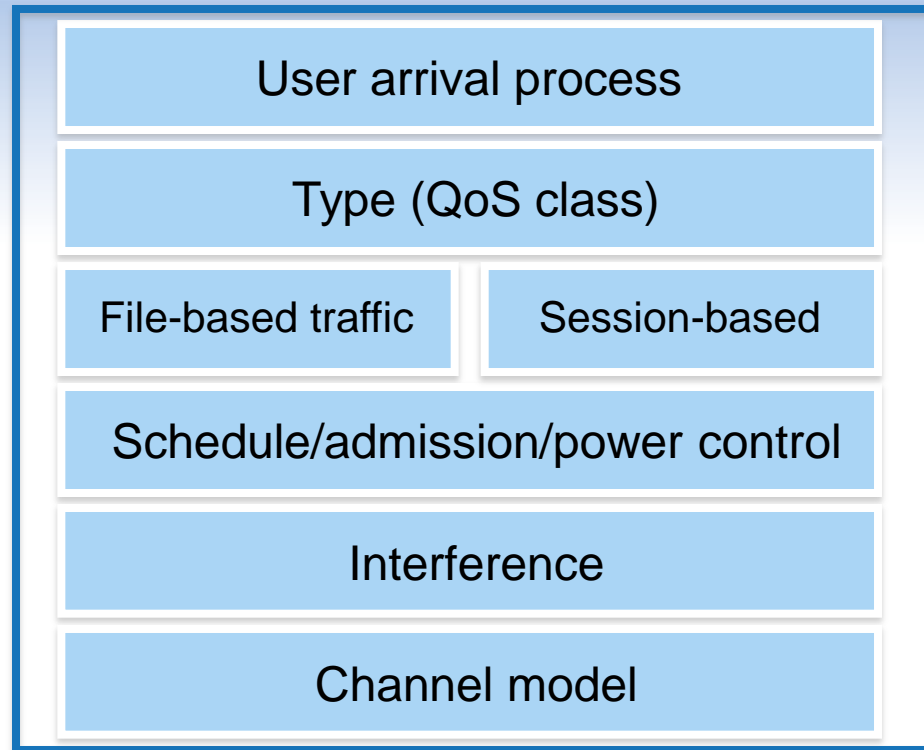
- Shannon + power function of d
- ...



“Construction toy” for UL performance prediction

Blocks:

Time



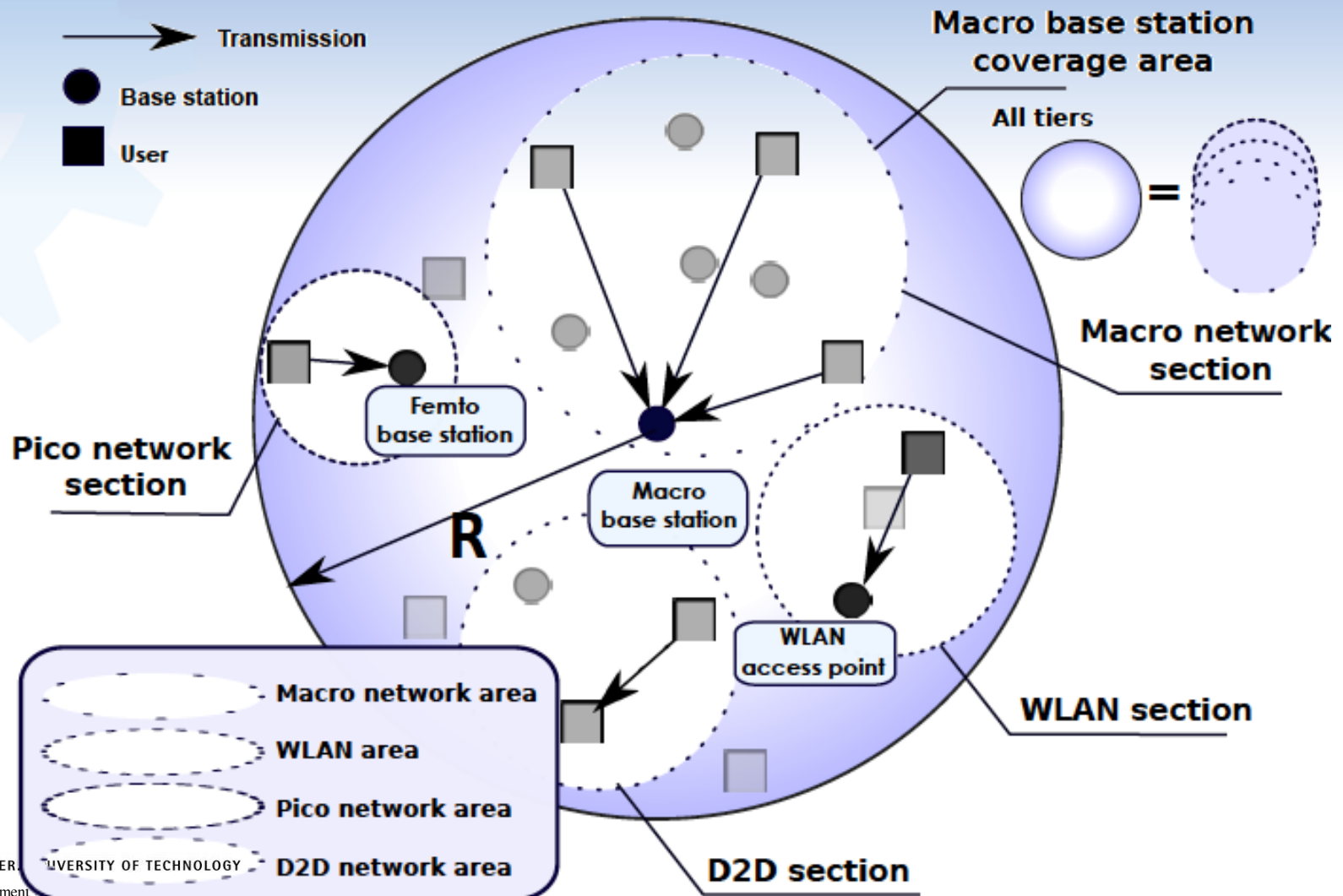
- Queueing system A/S/c/K/N/D
- Stationary distribution of ongoing users
- Averaged by space and time system characteristics



Heterogeneous network



Envisioned multitier network



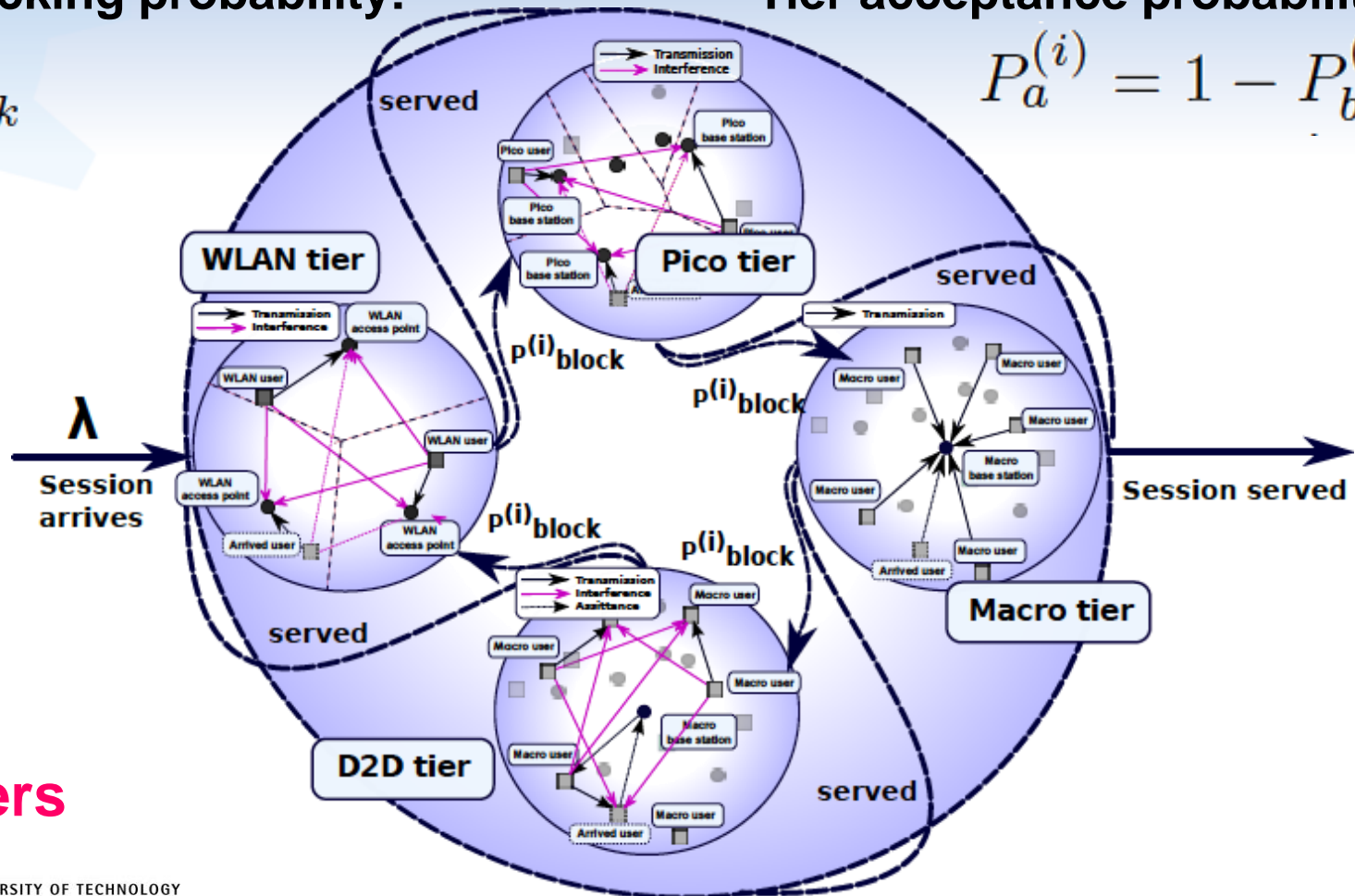
Example service discipline

Tier blocking probability:

$$P_{block}^{(i)}$$

Tier acceptance probability:

$$P_a^{(i)} = 1 - P_{block}^{(i)}$$



T tiers



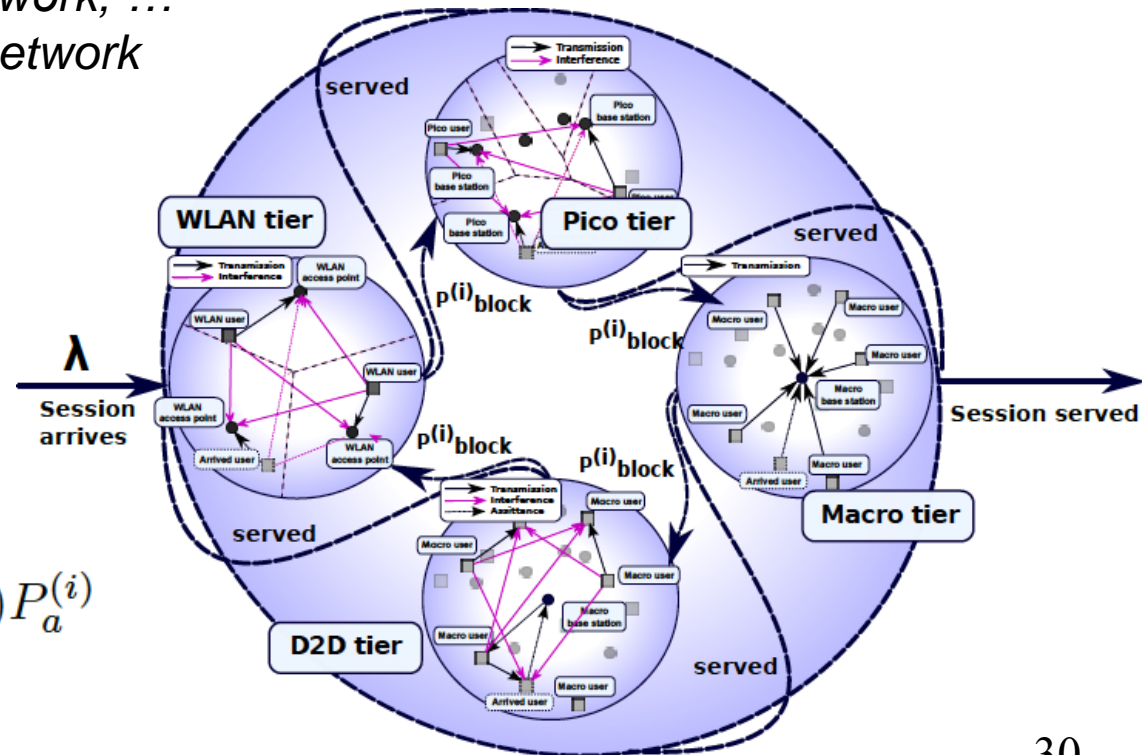
Multiple tiers

Several tiers based on diverse technologies: e.g., Macro cellular, WLAN, Pico cellular

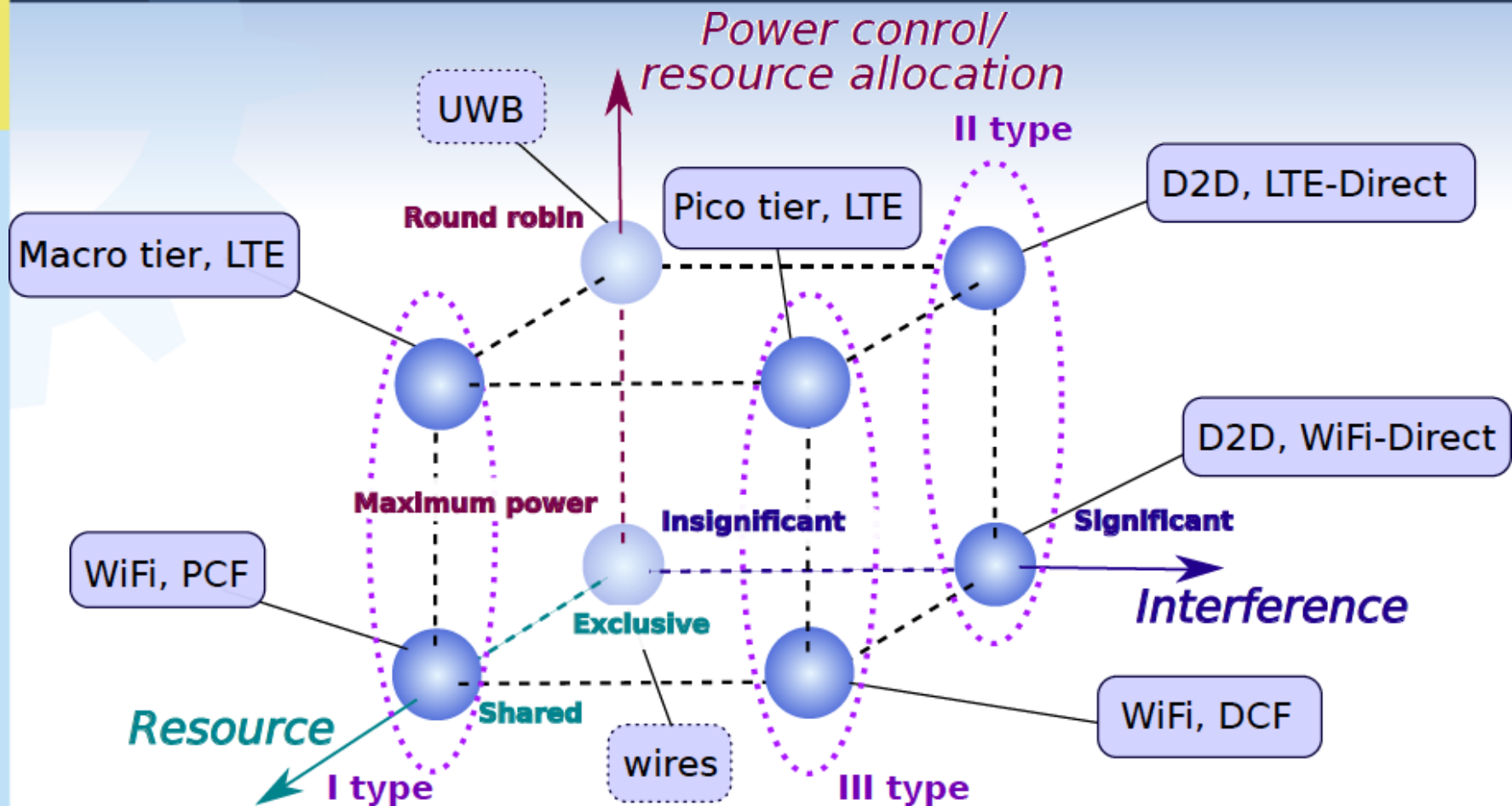
1. Attempt to offload new session onto the *D2D network* (by admission control).
2. If accepted, served by the network without interruption
3. Otherwise, attempt to *WLAN network*, ...
2. Otherwise, attempt to *Pico network*, ...
3. Otherwise, attempt to *Macro network*
4. If session is *not admitted*, it is considered **blocked**

System block probability:

$$P_{block} = 1 - \sum_{i=1}^T \prod_{j=1}^{i-1} (1 - P_a^{(j)}) P_a^{(i)}$$



Proposed taxonomy for HetNets



Example system model

Isolated cell of radius R:

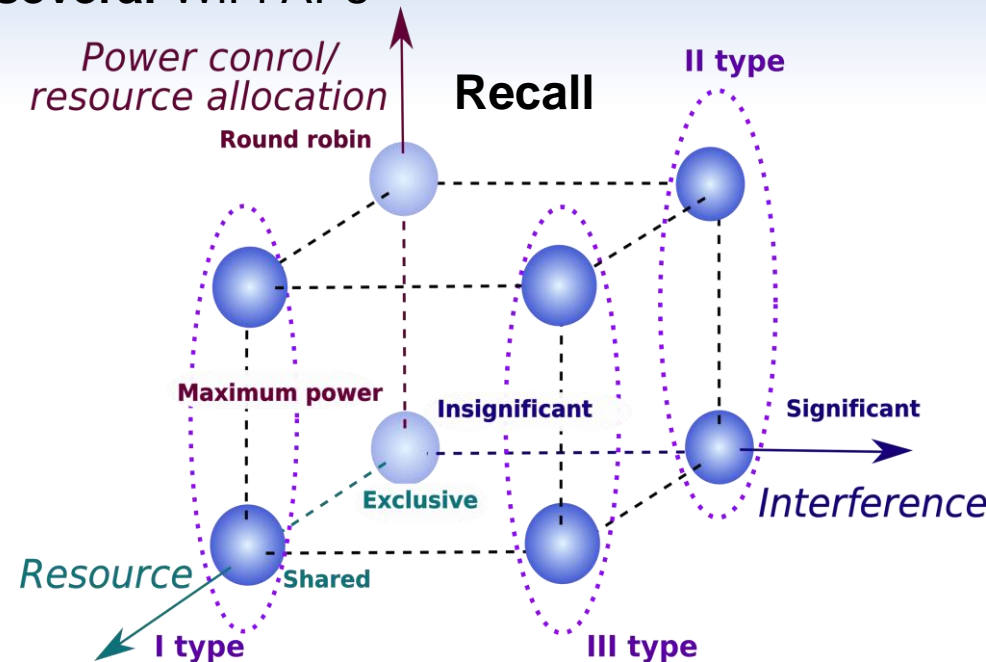
- macro BS + **several** femto BSs + **several** WiFi APs

Uplink, real-time sessions:

- Poisson arrivals of sessions, λ
- constant target bitrate, r_0
- and exponential holding time, μ
- or elastic traffic

• Three types of systems:

- Type I (no interference, shared resource)
- Type II (interference, exclusive resource)
- Type III (interference, shared resource)



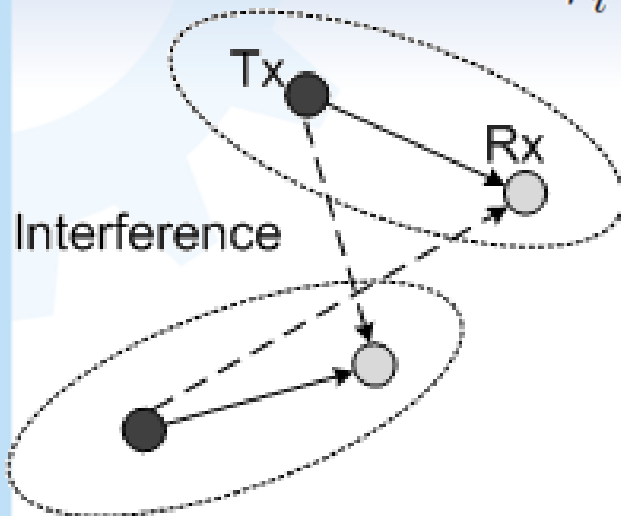
Are more complex and require further assumptions



Additional assumptions for T.II

Instantaneous rate Shannon's theorem for interference-limited environment

$$r_i = w \log \left(1 + SINR_i \right) = w \log \left(1 + \frac{P_i \gamma_{i,i}}{N_0 + I} \right)$$



Assumption

Noise plus interference power does not exceed some threshold

$$N_0 + I \leq KN_0$$

Assumption

D2D network of (**n-1**) users admits new session **n** if for the set of transmitters *at each receiver*.

$$\frac{P_{\max} \gamma_{i,i}}{KN_0} \geq e^{\frac{r}{w}} - 1$$

$$P_{\max} \gamma_{j,i} \leq N_0, \forall j, i \neq j$$

K is fixed throughout the D2D network



Transitions for T.I

We formulate Theorems connecting the obtained distributions and sought transitions rates

Theorem 1 For tier type I under the RR policy, the accept probabilities $\Pr\{\text{accepted} \mid \text{arrived}\} = 1 - Q_{n+1}$ can be obtained by:

$$1 - Q_{n+1} = \Pr\left\{r_{n+1}^{\max} \geq \frac{r_0(n+1)}{\delta_m}\right\} \left(\frac{\Pr\{r_i^{\max} \geq \frac{r_0}{\delta_m}(n+1)\}}{\Pr\{r_i^{\max} \geq \frac{r_0 n}{\delta_m}\}}\right)^n,$$

where

$$\Pr\{r \geq x\} = 1 - \Pr\{r < x\} = 1 - F_r(x),$$

and

$$F_r(x) = 1 - \frac{1}{R^2} \left[\frac{\eta G p}{N_0}\right]^{2/\kappa} (e^{r/w} - 1)^{-2/\kappa}, r_R \leq x < r_{lim}; \quad F_r(x) = 1, x \geq r_{lim}.$$



Transitions for T.II

Connections between the obtained distributions and sought transitions rates are dependent on the considered type

Theorem 2 *For tier type II under the MP policy, if admission control is performed according to (1.5) and, in particular, accounting for (1.14), then the reject probabilities Q_{n+1} can be closely approximated by:*

$$Q_{n+1} = 1 - \Pr\{\text{accepted} \mid \text{arrived}\} = \left[F_{\gamma} \left(\frac{N_0}{p_{\max}} \right) \right]^{2n-1} \left[1 - F_{\gamma} \left(\frac{\theta_0}{p_{\max}} \right) \right],$$

where $\theta_0 = KN_0 (e^{\frac{r}{w}} - 1)$ and the cumulative distribution function (CDF) for the SNR per a power unit γ is given as:

$$F_{\gamma}(\gamma) = 1 + \frac{G^{\frac{4}{k}} \gamma^{-\frac{4}{k}}}{8R^4} - \frac{G^{\frac{2}{k}} \gamma^{-\frac{2}{k}}}{R^2} \ln 2, \text{ if } \frac{G}{(2R^2)^{\frac{k}{2}}} \leq \gamma \leq \gamma_{\max}, \gamma_{\max} = \frac{KN_0}{p_{\max}} \left(e^{\frac{r_{\max}}{w}} - 1 \right)$$

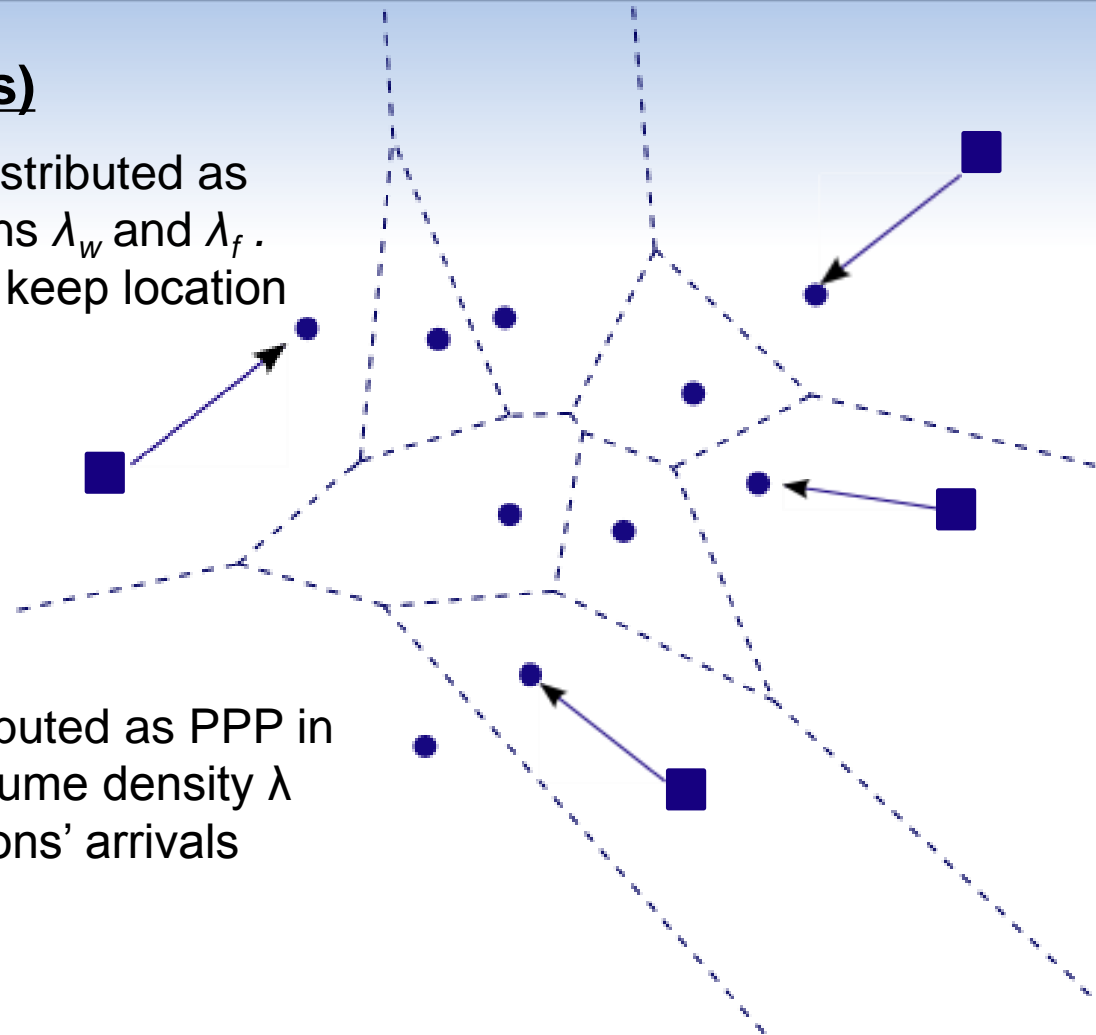
$$F_{\gamma}(\gamma) = 1 - \frac{1}{R^2} \left(\frac{G^{\frac{4}{k}} \gamma^{-\frac{4}{k}}}{8R^2} + G^{\frac{2}{k}} \gamma^{-\frac{2}{k}} \ln \frac{4R^2 \gamma^{\frac{2}{k}}}{G^{2k}} \right), \text{ if } \frac{G}{(2R)^k} \leq \gamma \leq \frac{G}{(2R^2)^{\frac{k}{2}}}.$$



Additional assumptions for T.III

Assumption (BS/AP locations)

APs and femto BSs are spatially distributed as PPP on **2D plane** with rate functions λ_w and λ_f . APs/BSs are considered fixed and keep location all the time during **one** realization.



Assumption (user location)

Users locations are spatially distributed as PPP in the 3D space ($X \times Y \times t$). We assume density λ for the time component (i.e. sessions' arrivals follow Poisson process of rate λ).

Additional assumptions for T.III

Assumption (admission control)

System admits *arrived session* if it has sufficient resources to serve it.
Each ongoing session i has to occupy exactly r_0/r_i of resource:

$$\sum_{\text{all sessions}} \left(\frac{r_0}{r_i} \right) \leq \delta$$

$\delta \leq 1$ – available resource

$r_i \leq r_{\max}$ - instantaneous data rate

r_{\max} - maximum achievable rate at the maximum power level.

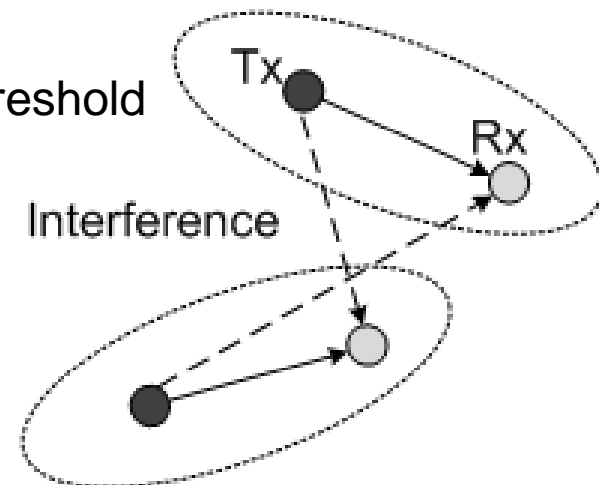
Assumption (interference)

Noise plus interference power does not exceed some threshold

$$N_0 + I \leq KN_0 \quad K \text{ is fixed}$$

Network of $(n-1)$ users admits new session n
if for the set of transmitters *at each receiver*:

$$p_j \gamma_{j,i} \leq N_0, \forall j, i \neq j$$



Transitions for T.III

Theorem 3 [Galinina et al. (2014)] For tier type III, the average number of sessions per receiver (AP/BS) n_0 tends to $\frac{n}{L_i(\pi R^2)} = \frac{n}{E[N_i]}$ for large areas, where $E[N_i]$ is the expected number of receivers of tier i within the circle R .

Theorem 4 For tier type III under the MP policy, the corresponding transition rates may be calculated as $\Pr\{\text{accepted} \mid \text{arrived}\} = 1 - Q_{n+1}$ accounting for the following:

$$1 - Q_{n+1} = \frac{\left(1 - e^{-\pi L_w d_{r,n+1}^2}\right)^{n+1}}{\left(1 - e^{-\pi L_w d_{r,n}^2}\right)^n} \left(L_w \pi d_{thr}^2 e^{-L_w \pi d_{thr}^2} + e^{-L_w \pi d_{thr}^2}\right),$$

where $d_{thr} = \left[\frac{G p_{\max}}{N_0}\right]^{\frac{1}{\kappa}}$ and the constant value $d_{r,n}$ is defined as $\left(\frac{p_{\max} \eta G}{K N_0}\right)^{\frac{1}{\kappa}} \left(e^{\frac{\tilde{r}_{0,n}}{w}} - 1\right)^{-\frac{1}{\kappa}}$.

$$\tilde{r}_{0,n} = r_0 / (\delta_w - \sigma_n) \quad \sigma_n = E \left[\frac{r_0}{r_i^{\max}} \mid \frac{r_0}{r_i^{\max}} \leq \delta_w \right] \frac{n}{E[N_i]} = E[y \mid y \leq \delta_i] \frac{n}{E[N_i]},$$

and $E[y \mid y \leq \delta_i]$ may be found as:

$$E[y \mid y \leq \delta_i] = \int_{y_0}^{\delta_i} y f_y(y \mid y \leq \delta_i) dy = \frac{\delta_i}{C_3} \int_{y_0}^{\delta_i} y d(y) d'(y) e^{-\pi L_w \left(\frac{p_{\max} \eta G}{K N_0}\right)^{\frac{2}{\kappa}} \left(\frac{r_0}{e^{wy} - 1}\right)^{-\frac{2}{\kappa}}} dy +$$

$$+ \frac{2\pi L_i}{C_3} y_0 \int_0^{y_0} d(y) d'(y) e^{-\pi L_w \left(\frac{p_{\max} \eta G}{K N_0}\right)^{\frac{2}{\kappa}} \left(\frac{r_0}{e^{wy} - 1}\right)^{-\frac{2}{\kappa}}} dy,$$

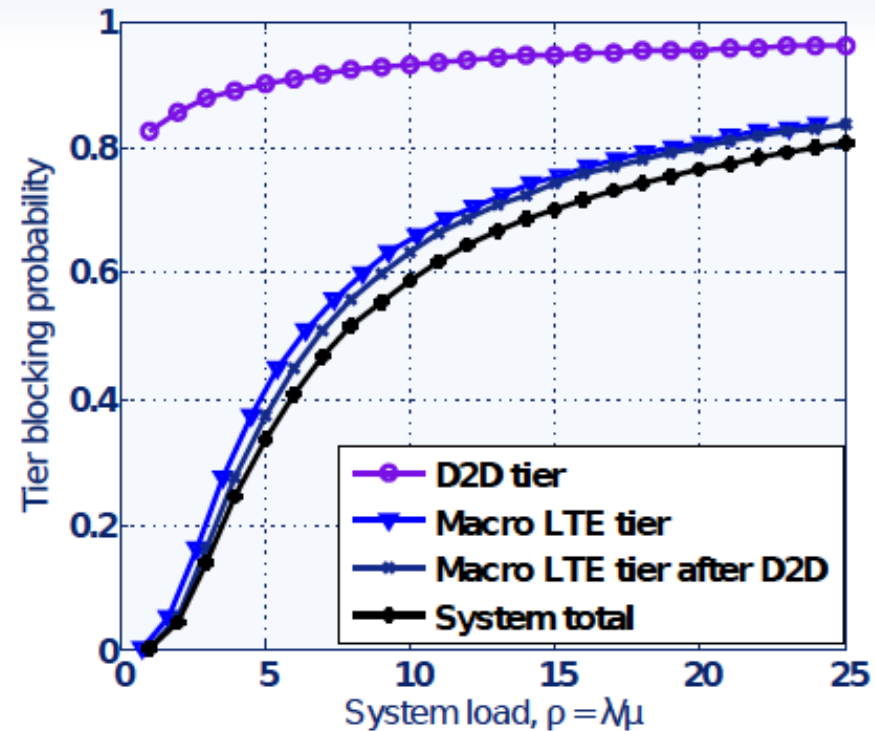
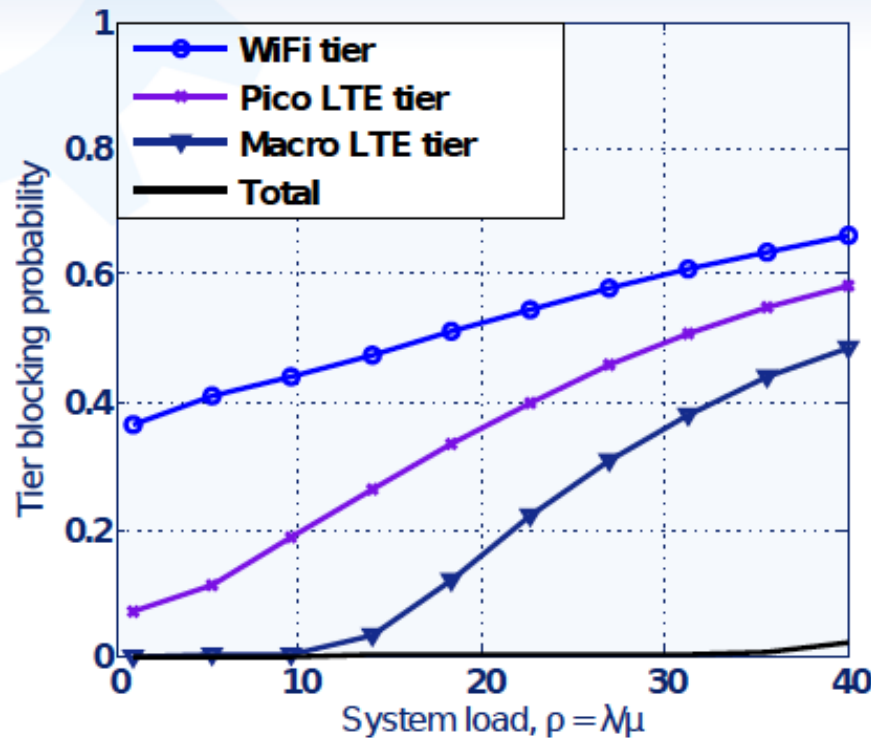


Numerical examples



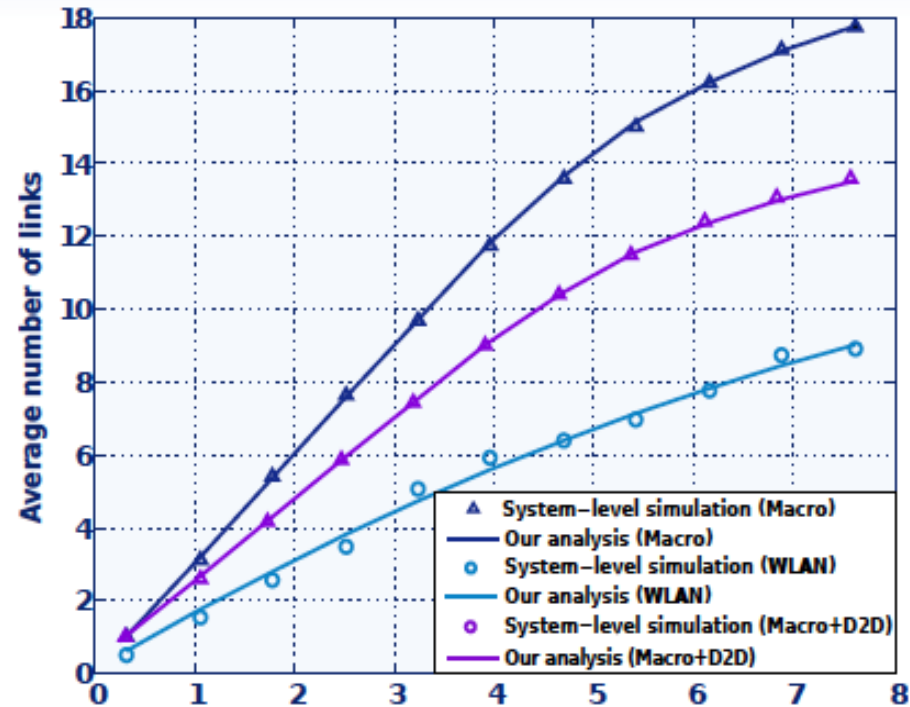
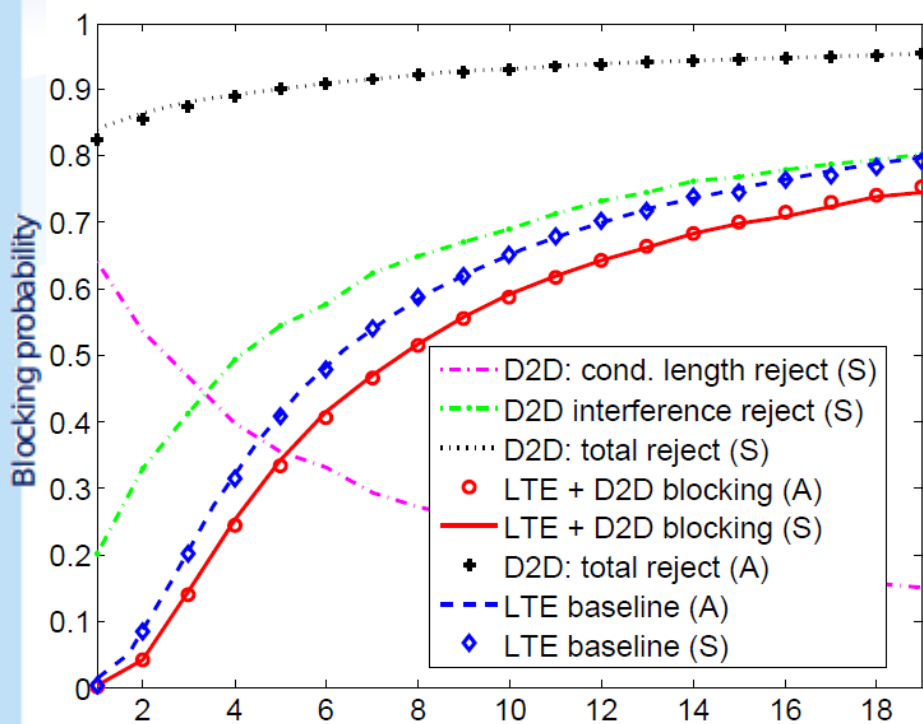
Numerical results 1/2

Analyzing blocking probabilities in:
three-tier (left), and **two-tier** (right) HetNets



Numerical results 2/2

Session **blocking/reject probabilities** (left) and **system capacity** (right)
vs. **system load**



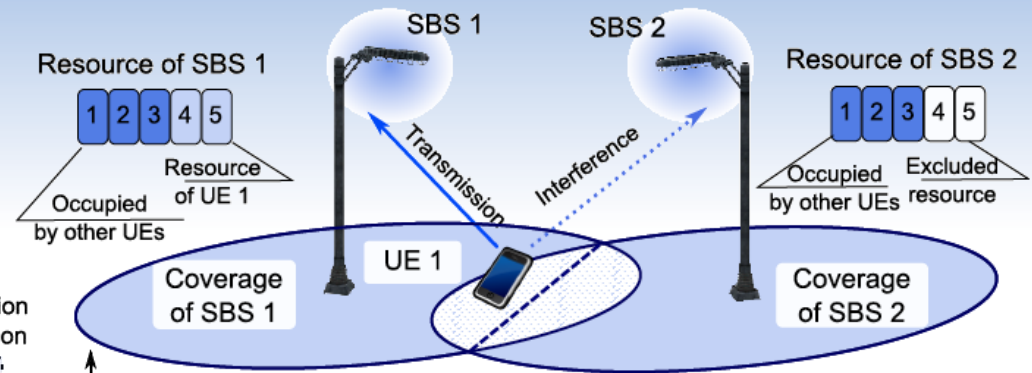
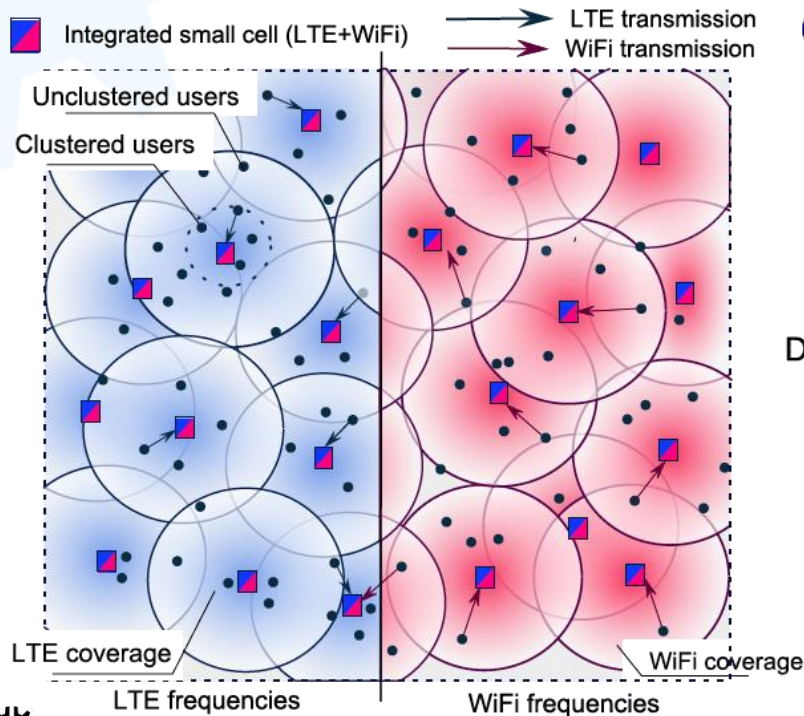
Main outcomes

- A unified mathematical methodology capturing :
 - the crucial HetNet dynamics, and
 - geometrical randomness of user deployment
- A classification of practical HetNet components
- Analytical methods of calculating main performance measures



Ultra-Dense Small Cells with co-located LTE and WiFi

Envisioned system topology



Interference coordination

Interference coordination

$$E \left[\frac{s_j}{\frac{\delta_w r_w}{i} + \frac{\delta_l r_l}{i}} \right]$$



Comparison co-located LTE and WiFi and WiFi-preferred scheme

Average transmission time for a file transfer

